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DECREASING REARRANGEMENT ON AVERAGE OPERATORS

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ABSTRACT. Let $\{T_{\theta}\}_{\theta}$ be a family of operators indexed in a probability measure space (Ω, \mathcal{A}, P) such that the boundedness

$$T_{\theta}: L^{1}(u) \longrightarrow L^{1,\infty}(u), \qquad \forall u \in A_{1},$$

holds with constant less than or equal to $\varphi(\|u\|_{A_1})$, with $\varphi:[1,\infty) \to (0,\infty)$ being an *admissible* function and where A_1 is the class of Muckenhoupt weights. The aim of this talk is to address the following question: what can we say about the decreasing rearrangement of the average operator

$$T_A f(x) = \int_{\Omega} T_{\theta} f(x) dP(\theta), \qquad x \in \mathbb{R}^n,$$

whenever is well defined?

This is a joint work with Elona Agora, Jorge Antezana and María J. Carro and it was done during the fulfillment of my doctoral thesis.

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