
(Research made in collaboration with C. de la Fuente Marcos, S. 1. Aarseth, de deon G. Carraro and E. Costà)
the remarks which Herschel entered in his Journal and reproduce a facsimile of the original record of the "comet" on March 13, 1781. The authors of this volume have also given a valuable discussion of the identification of the comet as a new planet.

The original entry in Herschel's Journal is as follows:- (the two vertical lines down the middle mean that the observations pave been copied into separate books for fixed stars, planets, etc.


Folly is follow) by
and $3^{\prime}$ distance.
on armual. PH

FROM HERSCHEL'S JOURNAL.
Sightly newest in ane.


After this original entry it was some days before Herschel could observe his comet again. On Thursday morning bethe five and six o'clock he observed Mars and Saturn, but apparently the sky
was not clear enough for him to hunt for the comet. He first saw it again on Saturday, March 17th, and we quote the following account from "Collected Scientific Papers," p. xxx. It shows that not only did Herschel fail to realize that he had found a new planet, but also, because of inaccuracy in his micrometers, he mistakenly thought the object was much nearer to us than it proved to be.


## THE NEW PLANET.

The discovery by M. Leverrier of a new planet beyond the boundaries of our solar system (as hitherto known), must rank as one of the most wonderful scientific nehievements of our time. From an extensive examination of the movements of Uranus, it had been for some time certain that it was affected by some unknown influence, and a conjecture was formed that a planet existed beyond it, disturbing its motions.

To M. Leverrier belongs the honour of the discovery. On the 31st of Angust he made public the elements of the orbit of the supposed planet, deduced by most laborious calculation from the observed disturbances. He also announced that the planet would probably present a dise of about 3 sec. in magnitude. This announcement reached Dr Galle, at Berlin, on the 23d of September, and on the same evening Dr Galle, on comparing the stara in Dr Bremiker's chart with the heavens, found a star of the eighth magnitude which was not marked upon the map, and this star eventually proved to be the expected new planet. M. Leverrier and M. Galle are both to receive from the King of the French crosses of the Legion of Honour for their grand discovery.

The present distance of the new planet, expressed in common measure, is about $3,200,000,000$ English miles from the sun, and about $3,100,000,000$ from the earth. Its distance from Uranus-whose motions it disturbs-is about $150,000,000$ of miles. Its diameter is estimated at 50,000 miles. That of Uranus is about 35,000; of Jupiter, 86,000; of Saturn, 79,000; of the Earth, 8000 . Its cubic bulk is to that of the earth as 250 to 1. The new planet is the largest in our system except Jupiter and Saturn; and since these two planets, as well as Uranus, are each attended by a train of satellites, it is extremely probable that the new planet will have a similar accompaniment. The planet comes to the meridian a few minutes before nine, and is within a short distanee of Saturn. With a power under 200, it is not distinguishable from a fixed star.

Mr Lassell, of Starfield, Liverpool, has written to state that he believes he can discern a ring surrounding the planet, and a star having every appearance of a satellite. The discovery of the ring and satellito is interesting, as completing that chain of uniformity and order we find pervading the whole creation. Thus the system of the universe, the work of Almighty inteliigonce, assists man in his researches, and onables him to proceed almost with certainty, from one discovery to another.

A fragment of Bremiker's celestial map on which a German hand (Galle's?) has plotted the position of Neptune predicted by Le Verrier (Neptun bereibnet) and the actual position (Neptun beobachtet). The position predicted by Adams is also indicated


# A Dynamical Search for a Transplutonian Planet 

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A dynamical search for three hypothetical planets having representative characteristics of transplutonian planets, but within certain magnitude limits, was made by numerical integration of the orbits of the outer planets with, and without, a hypothetical planet. Careful comparison of these orbits with observations indicates that, although there may be undiscovered planets beyond Neptune, their dynamical effect on the known planets is so small that their presence, or absence, cannot be clearly discerned from the observation residuals.

Mon. Not. R. astr. Soc. (1973) 162, 261-270.

MASS AND POSITION LIMITS FOR AN HYPOTHETICAL
TENTH PLANET OF THE SOLAR SYSTEM

## D. Rawlins and M. Hammerton

(Received 1972 December 20)

## SUMMARY

This paper describes an analysis of the residuals of Neptune, conducted in order to delimit the possible range of mass and position for an hypothetical tenth planet of the solar system. Classical perturbation theory was employed, using a least-squares fit to residual normals, the problem being simplified by assuming a circular orbit for any hypothetical body. Results are presented which offer a restricted range of possible values; and their possible significance is discussed.

# DYNAMICAL LIMITS ON DARK MASS IN THE OUTER SOLAR SYSTEM 

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#### Abstract

Dark matter in the outer solar system, such as a hypothetical Planet X or a Kuiper belt of material outside Neptune's orbit, may be detected by its dynamical influence on the orbits of the outer planets and comets. The study of simplified model solar systems with known observational errors offers insights into the best strategies to use in dynamical searches for dark mass, the significance of apparent anomalies, and the minimum detectable amounts of dark mass. We use this approach to establish the following results. (i) The inability of modern ephemerides to predict the longitude of Neptune accurately is a consequence of Neptune's long orbital period, and provides no evidence for the existence of dark mass. (ii) Searching for anomalous residuals when fitting observational data to models of the solar system that do not include dark mass is an inefficient way to detect dark mass; a more powerful test (by about a factor of 3-4) is to examine the improvement in fit when the observations are fitted to models that include dark mass. (iii) It is much harder to locate Planet X than to detect its existence: in order to predict the location of Planet $\mathbf{X}$ to within $1^{\circ}$ its mass must exceed about 10 times the minimum detectable mass. (iv) If Planet $X$ is massive and close enough to exert a detectable dynamical influence on the outer planets, then it is more likely than not that it would have been detected already in the IRAS survey. (v) Residuals in the orbits of comets such as Halley's are far more powerful probes for the Kuiper belt than are residuals in the orbits of the outer planets.


## The effect on the Edgeworth-Kuiper Belt of a large distant tenth planet

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ABSTRACT
We investigate the orbital evolution of both real and hypothetical Edgeworth-Kuiper Objects in order to determine whether any conclusions can be drawn regarding the existence, or otherwise, of the tenth planet postulated by Murray. We find no qualitative difference in the orbital evolution, and so conclude that the hypothetical planet has been placed on an orbit at such a large heliocentric distance that no evidence for the existence, or nonexistence, can be found from a study of the known Edgeworth-Kuiper Objects

Key words: celestial mechanics, stellar dynamics - minor planets, asteroids - Solar system: general.

# Biases in cometary catalogues and Planet $X$ 

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#### Abstract

Two sets of investigators - Murray and Matese et al. - have recently claimed evidence for an undiscovered Solar System planet from possible great circle alignments in the aphelia directions of the long-period comets. However, comet discoveries are bedevilled by selection effects. These include anomalies caused by the excess of observers in the Northern as against the Southern hemisphere, seasonal and diurnal biases, directional effects which make it harder to discover comets in certain regions of the sky, as well as sociological biases. A simple mathematical model is developed to illustrate the geometrical selection effects controlling comet discoveries. The stream proposed by Murray is shown on an equal-area Hammer-Aitoff projection. The addition of newer data weakens the case for the alignment. There is also evidence that the subsample in the stream is affected by seasonal and north-south biases. The stream proposed by Matese et al. is most obvious in the sample of dynamically new comets, and especially in those whose orbits are best known. The most recent data continue to maintain the overpopulation in the great circle. This pattern in the data occurs with a probability of only $\sim 1.5 \times 10^{-3}$ by chance. None of the known biases is able to provide such an alignment. Numerical integrations are used to demonstrate that a planet by itself can reduce the perihelia of comets in its orbital plane to sufficiently small values so that they could be discovered from the Earth. To maintain the observed flux of comets in the stream requires a parent population of $\sim 3 \times 10^{9}$ objects on orbits close to the planet's orbital plane. There is a need for a sample of long-period comets that is free from unknown or hard-to-model selection effects. Such will be provided by the European Space Agency satellite GAIA, which will discover $\sim 1000$ longperiod comets during its $5-\mathrm{yr}$ mission. This may finally bring to fruition the long tradition of looking for the effects of perturbers in cometary catalogues. Key words: stellar dynamics - celestial mechanics - comets: general - Kuiper Belt - Oort


 Cloud - planets and satellites: general.
# A SEARCH FOR A DISTANT COMPANION TO THE SUN WITH THE WIDE-FIELD INFRARED SURVEY EXPLORER* 

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#### Abstract

I have used multi-epoch astrometry from the Wide-field Infrared Survey Explorer to perform a search for a distant companion to the Sun via its parallactic motion. I have not found an object of this kind down to $W 2=14.5$. This limit corresponds to analogs of Saturn and Jupiter at 28,000 and 82,000 AU, respectively, according to models of the Jovian planets by Fortney and coworkers. Models of brown dwarfs by Burrows and coworkers predict fainter fluxes at a given mass for the age of the solar system, producing a closer distance limit of $26,000 \mathrm{AU}$ for a Jupiter-mass brown dwarf. These constraints exclude most combinations of mass and separation at which a solar companion has been suggested to exist by various studies over the years. Key words: brown dwarfs - infrared: planetary systems - planets and satellites: detection - proper motions - solar neighborhood




Figure 3. Detection limits for a companion to the Sun produced by current ( $R=21$ ) and future ( $R=26$ ) optical surveys and IR images from IRAS $\left(F_{12}=0.4 \mathrm{mJy}\right), 2 \mathrm{MASS}(J=16.6)$, and $\operatorname{WISE}(W 2=14.5)$. For the optical limits, objects with masses of $\geqslant 1 M_{\mathrm{Jup}}$ are assumed to have the same fluxes of reflected light because of their similar radii. The IR limits have been derived with fluxes predicted by models of brown dwarfs at an age of 5 Gyr (Burrows et al. 1997, 2003) and (for WISE only) models of Saturn and Jupiter in the absence of solar irradiation (Fortney et al. 2011).

## Orbits in the Solar System

In general, celestial bodies do not follow Keplerian orbits. Their current orbital states are described by osculating orbits or heliocentric (or barycentric) orbits in the absence of external perturbations.

## Orbits in the Solar System

Osculating orbits are characterized by:

- Size - semi-major axis (a)
- Shape - eccentricity (e)
perihelion distance $q=a(1-e)$ aphelion distance $Q=a(1+e)$
- Orientation in space inclination (i) $0^{0}-90^{\circ}$, direct $-90^{\circ}-180^{\circ}$, retrograde longitude of the ascending node ( $\Omega$ ) argument of perihelion ( $\omega$ )
longitude of perihelion parameter, $\varpi=\Omega+\omega$.


## Orbits in the Solar System



## Orbits in the Solar System

- The value of the semi-major axis defines the specific orbital energy and angular momentum (with e) of the object.
- The value of the eccentricity defines the specific orbital angular momentum (with a) of the object.
- The value of the inclination defines the angle between the orbital plane of the object and that of the ecliptic (Earth's orbit).
- In absence of external perturbations their values remain constant.


## Orbits in the Solar System

- For an unperturbed population of asteroids or comets, the values of the angular parameters (longitude of the ascending node, argument of perihelion and true anomaly, $f$ ) must be uniformly distributed, i.e. all the values are equally probable.
- External perturbations in the form of close encounters, and/or mean motion (and/or secular) resonances can transform a uniform distribution into any other.
- In absence of resonances the angular parameters circulate (can take any value); however, if resonances are at work, they may librate or oscillate (e.g. $\omega$ can librate about $0^{\circ}$ or $180^{\circ}$ ).


## Orbits in the Solar System

$$
\begin{aligned}
& \text { perihelion, } q \text {, and aphelion, } Q \text {, for the se objects. The coordinates of } \\
& \text { the perihelion, }\left(l_{q}, b_{q}\right) \text {, are given by the expressions (see e.g. Mur- } \\
& \text { ray \& Dermot } 1999) \text { : } \\
& \tan \left(l_{q}-\Omega\right)=\tan \omega \text { cos } i \text {, sin } b_{q}=\sin \omega \text { sin } i . \\
& \text { And the longitude and latitude of the aphelion are: } \\
& \left(l_{Q}, b_{Q}\right)=\left(l_{q}+180^{\circ},-b_{q}\right) \text {. } \\
& \text { In other words, objects with comparable values of } i, \Omega \text { and } \omega \text { have } \\
& \text { also very similar coordinates of both perihelion and aphelion. The } \\
& \text { three angular elements }-i, \Omega \text { and w specify the spatial orien- } \\
& \text { tation of the orbit. The analysis in Opik (1971) using cometary }
\end{aligned}
$$

Tomanov's Law. If the perihelia of a population of minor bodies are concentrated around a set of values, $\left(l_{q}, b_{q}\right)$, then a relation of the form:
$\tan i=\tan b_{q} / \sin \left(l_{q}-\Omega\right)$,
must exist between inclination and longitude of the ascending node.

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## ABSTRACT

The distribution of the axes defining the planes and orientations of the orbits of 542 long-period comets are analyzed. The directions of the perihelia and of the oriented plane normals show significant nonuniformity in their distributions. The preferred direction of perihelia near the apex of solar motion is refined to an ( $1 \sigma$ ) error circle of $20^{\circ} 6$, and possible concentrations of the plane normals and the directions of perihelion velocity along roughly orthogonal directions are noted, although the error circles extend to nearly full hemispheres. Planes of preference (and avoidance) are found from the distribution ellipsoids of the three orbital axes, with the perihelion directions lying preferentially along the galactic plane. The distribution ellipsoids of all three sets of orbital axes exhibit anisotropies roughly twice those expected for random distributions.
certain distances of one another are not, of course, independent. For $N$ random orbits. the mean number of pairs expected with plane normals differing by an angle less than $X$ and with perihelion directions differing by an angle less than $Y$ may be approximated, however, by

$$
\begin{equation*}
n_{2} \approx N(N-1) Y(1-\cos X) / 4 \pi \tag{lb}
\end{equation*}
$$

for small $X$.
 as instructive. The perihelion velocity direction, in particular, may reflect impulses received by the comet at aphelion, and it is surprising that it has been neglected in the statistical studies of the past.

## Evidence for an Extended Scattered Disk?



## Orbit Determination of 2000 CR105

2000 CR105 is a transneptunain object (in our Solar System's Kuiper Belt beyond Neptune), discovered in Febuary 2000 during a Kuiper Belt survey by a team at Lowell Observatory. We tracked the object in March 2000 from the Canada-France-Hawaii telescope and showed that the object's orbit was larger than any other known Kuiper Belt object, and in particular the fact that it's pericenter was farther from Neptune than any other highly-eccentric object. Since then we have continued to follow the object and have proven that its orbit is only weakly affected by the giant planets. A paper has been submitted to the journal Icarus describing the implications of this fact.

Evidence for an extended scattered disk
by
B. Gladman, M. Holman, T. Grav, J. Kavelaars, P. Nicholson, K. Aksnes, and J-M. Petit.

## Images

JPG images of 2000 CR105 in Normal black and white and Negative formats.


## ORBIT OF SCATTERED DISK OBJECTS AND 2000 CR 105

This figure compares the orbits of the other scattered disk objects with that we have estimated for 2000 CR105.

This figure shows the orbits of all the known scattered disk objects (SDOs) as well as the much larger orbit of 2000 CR105 (in red).
The SDOs are objects which are on large looping orbits; the most developed theories for the creation of the scattered disk produce these orbits by gravitational scattering due to Neptune, which hurls them out to external orbits which take hundreds of year to circulate around the Sun.
Numerical calculations have shown that some of the objects can rest in this state for the 4.5 -billion year lifetime of the Solar System.
The first recognized SDO was 1996 TL 66 , discovered by Luv et al. in 1996 (reprint in pdf format available on the www).
About two dozen such SDOs are now known, many of them have been discovered and tracked by C . Trujillo et al.

The figure shows that 2000 CR105 journeys far from the Sun, several times further than the other SDOs.
There are long-period comets that journey much farther away towards the
Oort cloud.
The interesting facet of CR105's orbit is NOT its large size, but rather the fact that its perihelion (distance of closest approach to the Sun) is larger than any other known Solar System object.

# Sedna, 2004 VN112 and 2000 CR105: the tip of an iceberg 

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#### Abstract

We review two main scenarios that may have implanted Sedna, 2004 VN112 and 2000 CR105 on their current peculiar orbits. These scenarios are based on perihelion lifting mechanisms that acted upon primordial scattered icy bodies. Supposing that the Sun was formed in a dense star cluster and that the gas giants were also forming while the cluster was still dense, an inner Oort cloud that includes Sedna at its inner edge could have been formed by the circularization of icy leftovers orbits scattered by the gas giants. A putative planetary mass solar companion can also produce a similar population of icy bodies through a perihelion lifting mechanism induced by secular resonances from the companion. A third scenario also dependent on a primordial dense cluster may contribute to adding a significant number of extrasolar icy bodies to the main solar component of the population created by the cluster model. These extrasolar objects are transferred to Sun orbits from the scattered disk of passing stars that were numerous in the dense primordial environment. We compare the scenarios as to the orbital distribution of the induced populations as well as their total mass. We conclude that both the cluster model and the solar companion model can produce icy body populations consistent with Sedna's orbit. It is also quite possible that this inner Oort cloud may be composed of roughly one tenth of extrasolar objects.


Keywords. Sedna, Oort cloud, star cluster, solar companion

## There is no compelling reason to believe that there are no planets beyond Pluto

- Observational data accumulated during the last decade do not explicitly rule out the presence of one or more super-Earth-sized planets at hundreds or thousands of AU from the Sun (see e.g. Luhman 2014; Batygin \& Brown 2016; Brown \& Batygin 2016; Fienga et al. 2016).
- The study of exo-planetary systems shows that planets moving in wide orbits do indeed exist (see e.g. Luhman et al. 2012; Bailey et al. 2014; Naud et al. 2014).
- Most exo-planets have masses below those of Uranus and Neptune but above that of the Earth (see e.g. Howard et al. 2010; Malhotra 2015; Silburt et al. 2015).


# A Sedna-like body with a perihelion of 80 astronomical units 

Chadwick A. Trujillo ${ }^{1 *}$ \& Scott S. Sheppard ${ }^{2 *}$

The observable Solar System can be divided into three distinct regions: the rocky terrestrial planets including the asteroids at 0.39 to 4.2 astronomical units ( AU ) from the Sun (where 1 AU is the mean distance between Earth and the Sun), the gas giant planets at 5 to 30 aU from the Sun, and the icy Kuiper belt objects at 30 to 50 AU from the Sun. The 1,000 -kilometre-diameter dwarf planet Sedna was discovered ten years ago and was unique in that its closest approach to the Sun (perihelion) is 76 AU , far greater than that of any other Solar System body ${ }^{1}$. Formation models indicate that Sedna could be a link between the Kuiper belt objects and the hypothesized outer Oort cloud at around $10,000 \mathrm{aU}$ from the $\mathrm{Sun}^{2-6}$. Here we report the presence of a second Sedna-likeobject, $2012 \mathrm{VP}_{113}$, whose perihelion is 80 AU . The detection of $2012 \mathrm{VP}_{113}$ confirms that Sedna is not an isolated object; instead, both bodies may be members of the inner Oort cloud, whose objects could outnumber all other dynamically stable populations in the Solar System.

The inner Oort cloud objects probably formed on nearly circular orbits, allowing them to accumulate mass efficiently ${ }^{6-9}$, and were later perturbed into the eccentric orbits we see today. We define an inner Oort cloud object as a body whose orbit is not readily formed with the known mass in the Solar System. This typically means a perihelion greater than 50 AU (beyond the range of significant Neptune interaction) and a semi-major axis in the range $150 \mathrm{AU}<a<1,500 \mathrm{AU}$. At above 1,500 aU objects may be considered to be in the outer Oort cloud, as galactic tides start to become important in the formation process ${ }^{10}$.


Figure $1 \mid$ Sedna and $2012 \mathrm{VP}_{113}$ are clear dynamical outliers in the Solar

# Extreme trans-Neptunian objects and the Kozai mechanism: signalling the presence of trans-Plutonian planets 

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#### Abstract

The existence of an outer planet beyond Pluto has been a matter of debate for decades and the recent discovery of $2012 \mathrm{VP}_{113}$ has just revived the interest for this controversial topic. This Sedna-like object has the most distant perihelion of any known minor planet and the value of its argument of perihelion is close to $0^{\circ}$. This property appears to be shared by almost all known asteroids with semimajor axis greater than 150 au and perihelion greater than 30 au (the extreme trans-Neptunian objects or ETNOs), and this fact has been interpreted as evidence for the existence of a super-Earth at 250 au . In this scenario, a population of stable asteroids may be shepherded by a distant, undiscovered planet larger than the Earth that keeps the value of their argument of perihelion librating around $0^{\circ}$ as a result of the Kozai mechanism. Here, we study the visibility of these ETNOs and confirm that the observed excess of objects reaching perihelion near the ascending node cannot be explained in terms of any observational biases. This excess must be a true feature of this population and its possible origin is explored in the framework of the Kozai effect. The analysis of several possible scenarios strongly suggest that at least two trans-Plutonian planets must exist.


Key words: celestial mechanics - minor planets, asteroids: general - minor planets, asteroids: individual: $2012 \mathrm{VP}_{113}$ - planets and satellites: individual: Neptune.

Table 1. Equatorial coordinates, apparent magnitudes (with filter if known) at discovery time, absolute magnitude, and $\omega$ for the 13 objects discussed in this Letter. (J2000.0 ecliptic and equinox. Source: MPC data base.)

| Object | $\alpha\left({ }^{\mathrm{h} . \mathrm{m} . \mathrm{s}}\right)$ | $\delta\left({ }^{\circ}:^{\prime}::^{\prime \prime}\right)$ | $m(\mathrm{mag})$ | $H(\mathrm{mag})$ | $\omega\left({ }^{\circ}\right)$ |
| :---: | :---: | :---: | :---: | :---: | ---: |
| 82158 | $11: 57: 50.69$ | $+00: 21: 42.7$ | $22.2(\mathrm{R})$ | 6.0 | 6.77 |
| Sedna | $03: 15: 10.09$ | $+05: 38: 16.5$ | $20.8(\mathrm{R})$ | 1.5 | 311.19 |
| 148209 | $09: 14: 02.39$ | $+19: 05: 58.7$ | $22.5(\mathrm{R})$ | 6.3 | 317.09 |
| $2002 \mathrm{~GB}_{32}$ | $12: 28: 25.94$ | $-00: 17: 28.4$ | $21.9(\mathrm{R})$ | 7.7 | 36.89 |
| $2003 \mathrm{HB}_{57}$ | $13: 00: 30.58$ | $-06: 43: 05.4$ | $23.1(\mathrm{R})$ | 7.4 | 10.64 |
| $2003 \mathrm{SS}_{422}$ | $23: 27: 48.15$ | $-09: 28: 43.4$ | $22.9(\mathrm{R})$ | 7.1 | 209.98 |
| $2004 \mathrm{VN}_{112}$ | $02: 08: 41.12$ | $-04: 33: 02.1$ | $22.7(\mathrm{R})$ | 6.4 | 327.23 |
| $2005 \mathrm{RH}_{52}$ | $22: 31: 51.90$ | $+04: 08: 06.1$ | $23.8(\mathrm{~g})$ | 7.8 | 32.59 |
| $2007 \mathrm{TG}_{422}$ | $03: 11: 29.90$ | $-00: 40: 26.9$ | 22.2 | 6.2 | 285.84 |
| $2007 \mathrm{VJ}_{305}$ | $00: 29: 31.74$ | $-00: 45: 45.0$ | 22.4 | 6.6 | 338.53 |
| $2010 \mathrm{~GB}_{174}$ | $12: 38: 29.365$ | $+15: 02: 45.54$ | $25.09(\mathrm{~g})$ | 6.5 | 347.53 |
| $2010 \mathrm{VZ}_{98}$ | $02: 08: 43.575$ | $+08: 06: 50.90$ | $20.3(\mathrm{R})$ | 5.0 | 313.80 |
| $2012 \mathrm{VP}_{113}$ | $03: 23: 47.159$ | $+01: 12: 01.65$ | $23.1(\mathrm{r})$ | 4.1 | 293.97 |



Figure 2. Frequency distribution in equatorial coordinates (right ascension, top panel, and declination, bottom panel) of the studied test orbits at perigee. The distribution is rather uniform in right ascension and shows a maximum for declinations in the range $-24^{\circ}$ to $24^{\circ}$. The bin sizes are 0.024 h in right ascension and 0.18 in declination, error bars are too small to be seen. The black circles correspond to objects in Table 1.


Figure 3. Frequency distribution in right ascension (bottom panel) and the orbital elements of test orbits with $|\delta|<24^{\circ}$. The bin sizes are 0.45 au in semimajor axis, 0.001 in eccentricity, 0.09 in inclination, 0.36 in longitude of the node, 0.36 in argument of perihelion and 0.024 h in right ascension, error bars are too small to be seen. The black circles correspond to objects in Table 1. Data from Table A1 have been used, this table is only available online.

## $\sqrt{1-e^{2}} \cos i=$ constant

# Flipping minor bodies: what comet 96P/Machholz 1 can tell us about the orbital evolution of extreme trans-Neptunian objects and the production of near-Earth objects on retrograde orbits 

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#### Abstract

Nearly all known extreme trans-Neptunian objects (ETNOs) have argument of perihelion close to $0^{\circ}$. An existing observational bias strongly favours the detection of ETNOs with arguments of perihelion close to $0^{\circ}$ and $180^{\circ}$ yet no objects have been found at $180^{\circ}$. No plausible explanation has been offered so far to account for this unusual pattern. Here, we study the dynamical evolution of comet 96P/Machholz 1, a bizarre near-Earth object (NEO) that may provide the key to explain the puzzling clustering of orbits around argument of perihelion close to $0^{\circ}$ recently found for the population of ETNOs. Comet 96P/Machholz 1 is currently locked in a Kozai resonance with Jupiter such that the value of its argument of perihelion is always close to $0^{\circ}$ at its shortest possible perihelion (highest eccentricity and lowest inclination) and about $180^{\circ}$ near its shortest aphelion (longest perihelion distance, lowest eccentricity and highest inclination). If this object is a dynamical analogue (albeit limited) of the known ETNOs, this implies that massive perturbers must keep them confined in orbital parameter space. Besides, its future dynamical evolution displays orbital flips when its eccentricity is excited to a high value and its orbit turns over by nearly $180^{\circ}$, rolling over its major axis. This unusual behaviour, that is preserved when post-Newtonian terms are included in the numerical integrations, may also help understand the production of NEOs on retrograde orbits.


Key words: relativistic processes - celestial mechanics - comets: individual: 96P/Machholz 1 - minor planets, asteroids: individual: $2012 \mathrm{VP}_{113}$ - planets and satellites: individual: Earth planets and satellites: individual: Jupiter.


Figure 2. Comparative short-term dynamical evolution of various parameters for the nominal orbit of comet 96P/Machholz 1 as presented in Table 2 (central panels) and two representative examples of orbits that are most different from the nominal one (see the text for details). The distance from Jupiter (A-panels); the value of the Hill sphere radius of Jupiter, 0.35 au , is displayed. The resonant angle, $\lambda_{\mathrm{r}}$ (B-panels). The orbital elements $a$ (C-panels), $e$ (D-panels), $i$ (E-panels) and $\omega$ (F-panels). The distances to the descending (thick line) and ascending nodes (dotted line) appear in the G-panels. Planetary aphelion and perihelion distances are also shown. The orbit labelled as 'nominal' is arbitrarily close to the nominal one but not that of Fig. 1.

# EVIDENCE FOR A DISTANT GIANT PLANET IN THE SOLAR SYSTEM 

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#### Abstract

Recent analyses have shown that distant orbits within the scattered disk population of the Kuiper Belt exhibit an unexpected clustering in their respective arguments of perihelion. While several hypotheses have been put forward to explain this alignment, to date, a theoretical model that can successfully account for the observations remains elusive. In this work we show that the orbits of distant Kuiper Belt objects (KBOs) cluster not only in argument of perihelion, but also in physical space. We demonstrate that the perihelion positions and orbital planes of the objects are tightly confined and that such a clustering has only a probability of $0.007 \%$ to be due to chance, thus requiring a dynamical origin. We find that the observed orbital alignment can be maintained by a distant eccentric planet with mass $\gtrsim 10 m_{\oplus}$ whose orbit lies in approximately the same plane as those of the distant KBOs, but whose perihelion is $180^{\circ}$ away from the perihelia of the minor bodies. In addition to accounting for the observed orbital alignment, the existence of such a planet naturally explains the presence of high-perihelion Sedna-like objects, as well as the known collection of high semimajor axis objects with inclinations between $60^{\circ}$ and $150^{\circ}$ whose origin was previously unclear. Continued analysis of both distant and highly inclined outer solar system objects provides the opportunity for testing our hypothesis as well as further constraining the orbital elements and mass of the distant planet.


Key words: Kuiper Belt: general - planets and satellites: dynamical evolution and stability


Figure 2. Orbital clustering in physical space. The right panels depicts the side and top views of the Keplerian trajectories of all bodies with $a>250 \mathrm{AU}$ as well as dynamically stable objects with $a>150 \mathrm{AU}$. The adopted color scheme is identical to that employed in Figure 1, and the two thin purple orbits correspond to stable bodies within the $150<a<250 \mathrm{AU}$ range. For each object, the directions of the angular momentum and Runge-Lenz (eccentricity) vectors are additionally shown. The left panel shows the location of perihelia of the minor bodies with $q>30 \mathrm{AU}$ and $a>50 \mathrm{AU}$ on the celestial sphere as points, along with the projection of their orbit poles with adjacent lines. The orbits with $a>250 \mathrm{AU}$ are emphasized in red. The physical confinement of the orbits is clearly evident in both panels.

We estimate the statistical significance of the observed clustering by assuming that the detection biases for our clustered objects are similar to the detection biases for the collection of all objects with $q>30 \mathrm{AU}$ and $a>50 \mathrm{AU}$. We then randomly select six objects from the sample 100,000 times and calculate the root mean square ( rms ) of the angular distance between the perihelion position of each object and the average perihelion position of the selected bodies. Orbits as tightly clustered in perihelion position as the six observed KBOs occur only $0.7 \%$ of the time. Moreover, the objects with clustered perihelia also exhibit clustering in orbital pole position, as can be seen by the nearly identical direction of their projected pole orientations. We similarly calculated the rms spread of the polar angles, and find that a cluster as tight as that observed in the data occurs only $1 \%$ of the time. The two measurements are statistically uncorrelated, and we can safely multiply the probabilities together to find that the joint probability of observing both the clustering in perihelion position and in pole orientation simultaneously is only $0.007 \%$. Even with only six objects currently in the group, the significance level is about $3.8 \sigma$. It is extremely unlikely that the objects are so tightly confined purely due to chance.

# OBSERVATIONAL CONSTRAINTS ON THE ORBIT AND LOCATION OF PLANET NINE <br> IN THE OUTER SOLAR SYSTEM 

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#### Abstract

We use an extensive suite of numerical simulations to constrain the mass and orbit of Planet Nine, the recently proposed perturber in a distant eccentric orbit in the outer solar system. We compare our simulations to the observed population of aligned eccentric high semimajor axis Kuiper belt objects (KBOs) and determine which simulation parameters are statistically compatible with the observations. We find that only a narrow range of orbital elements can reproduce the observations. In particular, the combination of semimajor axis, eccentricity, and mass of Planet Nine strongly dictates the semimajor axis range of the orbital confinement of the distant eccentric KBOs. Allowed orbits, which confine KBOs with semimajor axis beyond 380 au, have perihelia roughly between 150 and 350 au, semimajor axes between 380 and 980 au, and masses between 5 and 20 Earth masses. Orbitally confined objects also generally have orbital planes similar to that of the planet, suggesting that the planet is inclined approximately $30^{\circ}$ to the ecliptic. We compare the allowed orbital positions and estimated brightness of Planet Nine to previous and ongoing surveys which would be sensitive to the planet's detection and use these surveys to rule out approximately two-thirds of the planet's orbit. Planet Nine is likely near aphelion with an approximate brightness of $22<V<25$. At opposition, its motion, mainly due to parallax, can easily be detected within 24 hours.


Key words: celestial mechanics - Kuiper belt: general - planets and satellites: detection


Figure 10. Using all constraints on the orbital and physical parameters of Planet Nine, we can predict the location, distance, brightness, and speed of the planet throughout its orbit. Regions within $10^{\circ}$ of the galactic plane are outlined in red, and the ecliptic plane is shown in blue. The colored portions show regions where Planet Nine would have been or should be detected by previous or ongoing surveys. Light blue shows limits from the CRTS reanalysis, yellow shows Dark Energy Survey limits and coverage, dark blue shows Pan-STARRS transient analysis limits, green shows Pan-STARRS moving object analysis current limits, and red shows eventual Pan-STARRS expected limits. Orange shows the region exclusively ruled out by lack of observed perturbation to Saturn (Fienga et al. 2016; Holman \& Payne 2016). The black regions show regions of phase space where Planet Nine could not have been or will not be detected in previous or currently planned surveys.

As important as continued simulation, continued detection of distant solar system objects is the key to refining the orbital parameters of Planet Nine. Each addition KBO (or Centaur) with $a>100$ au tightens the observational constraints on the location of Planet Nine (or, alternatively, if significant numbers of objects are found outside of the expected cluster location, the obiects can refute the presence of a Planet Nine).

## Planet Nine hypothesis

Assuming a mass, $m$, in terms of the mass of the Earth:

- Semi-major axis (200 AU + $30 \mathrm{~m}, 600 \mathrm{AU}+20 \mathrm{~m}$ ) if $m=10$ Earth masses $\rightarrow(500 \mathrm{AU}, 800 \mathrm{AU})$
- Eccentricity $=0.75-((250 \mathrm{AU}+20 \mathrm{~m}) / \mathrm{a})^{8}$ if $m=10$ Earth masses $\rightarrow(0.32,0.74)$
- Inclination $\left(22^{\circ}, 40^{\circ}\right)$
- Longitude of the ascending node $\left(72^{\circ}, 121^{\circ}\right)$
- Argument of perihelion $\left(120^{\circ}, 160^{\circ}\right)$


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# Dynamical impact of the Planet Nine scenario: $N$-body experiments 

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#### Abstract

The Planet Nine hypothesis has now enough constraints to deserve further attention in the form of detailed numerical experiments. The results of such studies can help us improve our understanding of the dynamical effects of such a hypothetical object on the extreme transNeptunian objects or ETNOs and perhaps provide additional constraints on the orbit of Planet Nine itself. Here, we present the results of direct $N$-body calculations including the latest data available on the Planet Nine conjecture. The present-day orbits of the six ETNOs originally linked to the hypothesis are evolved backwards in time and into the future under some plausible incarnations of the hypothesis to investigate if the values of several orbital elements, including the argument of perihelion, remain confined to relatively narrow ranges. We find that a nominal Planet Nine can keep the orbits of (90377) Sedna and $2012 \mathrm{VP}_{113}$ relatively well confined in orbital parameter space for hundreds of Myr, but it may make the orbits of $2004 \mathrm{VN}_{112}, 2007$ $\mathrm{TG}_{422}$ and $2013 \mathrm{RF}_{98}$ very unstable on time-scales of dozens of Myr, turning them retrograde and eventually triggering their ejection from the Solar system. Far more stable orbital evolution is found with slightly modified orbits for Planet Nine.


Key words: methods: numerical - celestial mechanics - Kuiper belt: general - minor planets, asteroids: general-Oort Cloud - planets and satellites: general.


Figure 2. Orbital evolution of the six ETNOs in Table 1 subjected to th
Figure 5. Orbital evolution into the future for a representative solution with $\Delta \Omega=0^{\circ}$ and $\Delta \omega=180^{\circ}$ (see the text for details). Colours as in Fig. 2. nominal Planet Nine perturbation (see the text for details): (90377) Sedn (black), $2004 \mathrm{VN}_{112}$ (orange), $2007 \mathrm{TG}_{422}$ (blue), $2010 \mathrm{~GB}_{174}$ (purple), 2012 VP $_{113}$ (grey) and 2013 RF98 (red).


Figure 3. Detail of the pre-ejection evolution of $2007 \mathrm{TG}_{422}$ for a simulation different from the one displayed in Fig. 2.

# Finding Planet Nine: apsidal anti-alignment Monte Carlo results 

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#### Abstract

The distribution of the orbital elements of the known extreme trans-Neptunian objects or ETNOs has been found to be statistically incompatible with that of an unperturbed asteroid population following heliocentric or, better, barycentric orbits. Such trends, if confirmed by future discoveries of ETNOs, strongly suggest that one or more massive perturbers could be located well beyond Pluto. Within the trans-Plutonian planets paradigm, the Planet Nine hypothesis has received much attention as a robust scenario to explain the observed clustering in physical space of the perihelia of seven ETNOs which also exhibit clustering in orbital pole position. Here, we revisit the subject of clustering in perihelia and poles of the known ETNOs using barycentric orbits, and study the visibility of the latest incarnation of the orbit of Planet Nine applying Monte Carlo techniques and focusing on the effects of the apsidal anti-alignment constraint. We provide visibility maps indicating the most likely location of this putative planet if it is near aphelion. We also show that the available data suggest that at least two massive perturbers are present beyond Pluto.


Key words: methods: statistical-celestial mechanics - minor planets, asteroids: generalOort Cloud - planets and satellites: detection - planets and satellites: general.

The resonant coupling mechanism described in Batygin \& Brown (2016) emphasizes the existence of simultaneous apsidal antialignment and nodal alignment, i.e. $\Delta \varpi$ librates about $180^{\circ}$ and $\Delta \Omega$ librates about $0^{\circ}$. The relative values of $\omega$ and $\Omega$ of the ETNO with respect to those of the perturber must oscillate in order to maintain orbital confinement but see Beust (2016) for a detailed analysis. In Batygin \& Brown (2016), the value of $\omega$ of the putative


Figure 3. Distribution in equatorial coordinates of the aphelia of the studied orbits as a function of various orbital parameters: $Q$ (panel A), $a$ (panel B), $e$ (panel C), $i$ (panel D), $\Omega$ (panel E), and $\omega$ (panel F). The left-hand panels show results using the sets of orbits in Batygin \& Brown (2016), those of orbits from Brown \& Batygin (2016) are displayed in the second to left-hand panels; the second to right-hand panels and the right-hand panels focus on the set of orbits described in Section 3.3, imposing $\Delta \omega \sim 180^{\circ}$ and $\Delta \Omega \sim 0^{\circ}$ using the data in Tables 2 and A1, respectively. In panel D, the green circles give the location at discovery of known ETNOs (see table 2 in de la Fuente Marcos \& de la Fuente Marcos 2016a), in red we have the Galactic disc that is arbitrarily defined as the region confined between galactic latitude $-5^{\circ}$ and $5^{\circ}$, in pink the region enclosed between galactic latitude $-30^{\circ}$ and $30^{\circ}$, and in black the ecliptic.

# CONSEQUENCES OF A DISTANT MASSIVE PLANET ON THE LARGE SEMIMAJOR AXIS TRANSNEPTUNIAN OBJECTS 

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#### Abstract

We explore the distant giant planet hypothesis by integrating the large-semimajor-axis, large-pericenter transNeptunian objects (TNOs) in the presence of the giant planets and an external perturber whose orbit is consistent with the proposed distant, eccentric, and inclined giant planet, so-called planet 9 . We find that TNOs with semimajor axes greater than 250 au experience some longitude of perihelion shepherding, but that a generic outcome of such evolutions is that the TNOs evolve to larger pericenter orbits and commonly get raised to retrograde inclinations. This pericenter and inclination evolution requires a massive disk of TNOs (tens of $M_{\oplus}$ ) in order to explain the detection of the known sample today. Some of the highly inclined orbits produced by the examined perturbers will be inside of the orbital parameter space probed by prior surveys, implying a missing signature of the ninth-planet scenario. The distant giant planet scenarios explored in this work do not reproduce the observed signal of simultaneous clustering in argument of pericenter, longitude of the ascending node, and longitude of perihelion in the region of the known TNOs.


Key words: Kuiper belt: general - planet-disk interactions


Figure 7. The $i, q$ evolution of the Sedna clones for the various P9 configurations. Clones from the simulation with $i=30^{\circ}$ are shown in blue, $\mathrm{P} 9 i=15^{\circ}$ in red, and P9 $i=0^{\circ}$ in magenta. A dashed gray line marks $i=90^{\circ}$ in panel (a). Panel (a) shows that the same $i$ raising and flipping is induced for $\varpi$-shepherded clones in both the P9 $i=30^{\circ}$ and $\mathrm{P} 9 i=15^{\circ}$ cases. Panel (b) shows that large- $q$ oscillations occur for $\varpi$-shepherded clones in all simulations. The cycling of $q$ is a generic feature of a massive external perturber, regardless of the perturber's inclination. Inclination raising occurs generically for $\varpi$ shepherded clones in the simulations with high ( $30^{\circ}$ ) and more moderate $\left(15^{\circ}\right)$ perturber inclinations.
 currently missing or unseen signature of P9. The P9 scenario does not produce the observed simultaneous clustering in the angles $\omega, \Omega$, and $\varpi$ that is seen in the detected sample. Taken

# Commensurabilities between ETNOs: a Monte Carlo survey 

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#### Abstract

Many asteroids in the main and trans-Neptunian belts are trapped in mean motion resonances with Jupiter and Neptune, respectively. As a side effect, they experience accidental commensurabilities among themselves. These commensurabilities define characteristic patterns that can be used to trace the source of the observed resonant behaviour. Here, we explore systematically the existence of commensurabilities between the known ETNOs using their heliocentric and barycentric semimajor axes, their uncertainties, and Monte Carlo techniques. We find that the commensurability patterns present in the known ETNO population resemble those found in the main and trans-Neptunian belts. Although based on small number statistics, such patterns can only be properly explained if most, if not all, of the known ETNOs are subjected to the resonant gravitational perturbations of yet undetected trans-Plutonian planets. We show explicitly that some of the statistically significant commensurabilities are compatible with the Planet Nine hypothesis; in particular, a number of objects may be trapped in the 5:3 and 3:1 mean motion resonances with a putative Planet Nine with semimajor axis $\sim 700$ au.


Key words: methods: statistical - celestial mechanics - Kuiper belt: general - minor planets, asteroids: general - Oort Cloud - planets and satellites: general.

Ignoring the mass of the object, expressing distances in astronomical units, times in sidereal years, and masses in Solar masses, Kepler's Third Law applied to an object orbiting the Sun states that $P^{2}=$ $a^{3}$, where $P$ is the period and $a$ is the semimajor axis of the orbit of the object. Given two objects - the first one with $a_{i}$ and $P_{i}$, and the second one with $a_{j}$ and $P_{j}, i \neq j-$ Kepler's Third Law is given by $\left(P_{j} / P_{i}\right)^{2}=\left(a_{j} / a_{i}\right)^{3}$. If $P_{j} / P_{i}$ can be written in the form of a ratio of small integers then we have a mean motion resonance. In order to investigate the distribution of ratios of orbital periods, $P_{j} / P_{i}$, for the ETNOs the values of the semimajor axes are needed.



Figure 1. Commensurability map (top panel) for the values of the heliocentric semimajor axes and their uncertainties in Table 1. Frequency distribution (bottom panel) in $\left(a_{j} / a_{i}\right)^{3 / 2}$ from the commensurability map. The results from a uniform spread in semimajor axis are plotted in purple and those from a biased uniform sample in green. The number of bins in the frequency distribution plot is $2 n^{1 / 3}$, where $n$ is the number of pairs of virtual ETNOs tested, $n=10^{6}$. The black curve shows the cumulative distribution.

If the mechanisms responsible for inducing dynamical structure in the main and trans-Neptunian belts are also at work in the region occupied by the ETNOs then we should expect that for two given ETNOs in near commensurability:

$$
\begin{equation*}
\left(\frac{a_{\mathrm{p}}}{a_{j}}\right)^{3 / 2}\left(\frac{a_{i}}{a_{\mathrm{p}}}\right)^{3 / 2}=\left(\frac{m}{n}\right)\left(\frac{k}{l}\right) \tag{1}
\end{equation*}
$$

where $a_{\mathrm{p}}$ is the semimajor axis of the orbit of the perturber and $k, l$, $m, n$ are all small integers. This expression can be applied to two of the most clear clusterings in semimajor axis in Table 2. The average value of the barycentric semimajor axis of (90377) Sedna and 2007 $\mathrm{TG}_{422}$ is 504 au . On the other hand, the equivalent mean value for $2004 \mathrm{VN}_{112}$, $2010 \mathrm{~GB}_{174}$ and $2013 \mathrm{RF}_{98}$ is 332 au . These five objects are part of the set of six singled out by Batygin \& Brown (2016). The associated period ratio for these two sets of ETNOs is 1.87 . In the main asteroid belt, this ratio is obtained for objects trapped in the 5:3 mean motion resonance with Jupiter and those in the 3:1, that is one of the main resonances in the outer belt (Holman \& Murray 1996). Making a dynamical analogy between the two situations and decomposing equation (1) in two we have: $\left(a_{\mathrm{p}} / 504\right)^{3 / 2}=5 / 3$ and $\left(332 / a_{\mathrm{p}}\right)^{3 / 2}=1 / 3$. The average of the two values of $a_{\mathrm{p}}$ is $\sim 700$ au which is the favoured value for the semimajor axis of Planet Nine in Batygin \& Brown (2016). The 1.8 commensurability has a statistical significance of $239 \sigma$ for heliocentric orbits, the 1.89 commensurability has $51 \sigma$ for barycentric orbits (see Fig. 3). This is unlikely to be mere coincidence.

# NEW EXTREME TRANS-NEPTUNIAN OBJECTS: TOWARD A SUPER-EARTH IN THE OUTER SOLAR SYSTEM 

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#### Abstract

We are performing a wide and deep survey for extreme distant solar system objects. Our goal is to understand the high-perihelion objects Sedna and 2012 VP113 and determine if an unknown massive planet exists in the outer solar system. The discovery of new extreme objects from our survey of some 1080 square degrees of sky to over 24th magnitude in the $r$-band are reported. Two of the new objects, 2014 SR349 and 2013 FT28, are extreme detached trans-Neptunian objects, which have semimajor axes greater than 150 au and perihelia well beyond Neptune ( $q>40 \mathrm{au}$ ). Both new objects have orbits with arguments of perihelia within the range of the clustering of this angle seen in the other known extreme objects. One of these objects, 2014 SR349, has a longitude of perihelion similar to the other extreme objects, but 2013 FT28 is about $180^{\circ}$ away or anti-aligned in its longitude of perihelion. We also discovered the first outer Oort Cloud object with a perihelion beyond Neptune, 2014 FE72. We discuss these and other interesting objects discovered in our ongoing survey. All the high semimajor axis ( $a>150 \mathrm{au}$ ) and high-perihelion ( $q>35 \mathrm{au}$ ) bodies follow the previously identified argument of perihelion clustering as first reported and explained as being from an unknown massive planet in 2014 by Trujillo \& Sheppard, which some have called Planet X or Planet Nine. With the discovery of 2013 FT28 on the opposite side of the sky, we now report that the argument of perihelion is significantly correlated with the longitude of perihelion and orbit pole angles for extreme objects and find there are two distinct extreme clusterings anti-aligned with each other. This previously unnoticed correlation is further evidence of an unknown massive planet on a distant eccentric inclined orbit, as extreme eccentric objects with perihelia on opposite sides of the sky ( $180^{\circ}$ longitude of perihelion differences) would approach the inclined planet at opposite points in their orbits, thus making the extreme objects prefer to stay away from opposite ecliptic latitudes to avoid the planet (i.e., opposite argument of perihelia or orbit pole angles).


Key words: comets: general - Kuiper belt: general - minor planets, asteroids: general - Oort Cloud planets and satellites: individual (Sedna, 2012 VP113)



Table 1. Equatorial coordinates ( $\alpha, \delta, \mathrm{J} 2000.0$ ecliptic and equinox), ap parent magnitudes ( $m$, with filter if known) at discovery time, and absolut, magnitude, $H$, for the 21 known ETNOs. Source: MPC Database.

| Object | $\begin{gathered} \alpha \\ (\mathrm{h} \cdot \mathrm{~m} \cdot \mathrm{~s}) \end{gathered}$ | $\begin{gathered} \delta \\ \left({ }^{\circ}:!^{\prime \prime}:^{\prime \prime}\right) \end{gathered}$ | $\begin{gathered} m \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} H \\ (\mathrm{mag}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| (82158) $2001 \mathrm{FP}_{185}$ | 11:57:50.69 | +00:21:42.7 | 22.2 (R) | 6.0 |
| (90377) Sedna | 03:15:10.09 | +05:38:16.5 | 20.8 (R) | 1.5 |
| (148209) $2000 \mathrm{CR}_{105}$ | 09:14:02.39 | +19:05:58.7 | 22.5 (R) | 6.3 |
| (445473) $2010 \mathrm{VZ}_{98}$ | 02:08:43.575 | +08:06:50.90 | 20.3 (R) | 5.0 |
| (474640) $2004 \mathrm{VN}_{112}$ | 02:08:41.12 | -04:33:02.1 | 22.7 (R) | 6.4 |
| 2002 GB32 | 12:28:25.94 | -00:17:28.4 | 21.9 (R) | 7.7 |
| 2003 HB 57 | 13:00:30.58 | -06:43:05.4 | 23.1 (R) | 7.4 |
| $2003 \mathrm{SS}_{422}$ | 23:27:48.15 | -09:28:43.4 | 22.9 (R) | 7.1 |
| $2005 \mathrm{RH}_{52}$ | 22:31:51.90 | +04:08:06.1 | 23.8 (g) | 7.8 |
| $2007 \mathrm{TG}_{422}$ | 03:11:29.90 | -00:40:26.9 | 22.2 | 6.2 |
| $2007 \mathrm{VJ}_{305}$ | 00:29:31.74 | -00:45:45.0 | 22.4 | 6.6 |
| 2010 GB 174 | 12:38:29.365 | +15:02:45.54 | 25.09 (g) | 6.5 |
| $2012 \mathrm{VP}_{113}$ | 03:23:47.159 | +01:12:01.65 | 23.1 (r) | 4.1 |
| $2013 \mathrm{FS}_{28}$ | 12:58:03.652 | -08:18:12.61 | 24.4 (r) | 4.9 |
| $2013 \mathrm{FT}_{28}$ | 12:44:55.262 | -12:28:17.85 | 24.4 (r) | 6.7 |
| $2013 \mathrm{GP}_{136}$ | 14:07:32.880 | -11:09:38.81 | 22.9 (r) | 6.6 |
| 2013 RF98 | 02:29:07.61 | -04:56:34.6 | 23.5 (z) | 8.6 |
| $2013 \mathrm{UH}_{15}$ | 01:38:30.772 | -02:46:20.79 | 24.8 (r) | 7.7 |
| $2014 \mathrm{FE}_{72}$ | 12:09:10.566 | -12:59:00.28 | 23.9 (r) | 6.1 |
| 2014 SR $_{349}$ | 22:17:39.955 | -28:55:52.76 | 24.1 (r) | 6.6 |
| $2015 \mathrm{SO}_{20}$ | 01:01:17.301 | -03:11:00.81 | 21.4 (R) | 6.5 |

# Visible spectra of (474640) $2004 \mathrm{VN}_{112}-2013$ RF $_{98}$ with OSIRIS at the $\mathbf{1 0 . 4} \mathbf{~ m}$ GTC: evidence for binary dissociation near aphelion among the extreme trans-Neptunian objects 

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#### Abstract

The existence of significant anisotropies in the distributions of the directions of perihelia and orbital poles of the known extreme trans-Neptunian objects (ETNOs) has been used to claim that trans-Plutonian planets may exist. Among the known ETNOs, the pair (474640) 2004 $\mathrm{VN}_{112}-2013 \mathrm{RF}_{98}$ stands out. Their orbital poles and the directions of their perihelia and their velocities at perihelion/aphelion are separated by a few degrees, but orbital similarity does not necessarily imply common physical origin. In an attempt to unravel their physical nature, visible spectroscopy of both targets was obtained using the OSIRIS camera-spectrograph at the 10.4 m Gran Telescopio Canarias (GTC). From the spectral analysis, we find that 474640-2013 $\mathrm{RF}_{98}$ have similar spectral slopes ( 12 versus 15 per cent/ $0.1 \mu \mathrm{~m}$ ), very different from Sedna's but compatible with those of (148209) $2000 \mathrm{CR}_{105}$ and $2012 \mathrm{VP}_{113}$. These five ETNOs belong to the group of seven linked to the Planet Nine hypothesis. A dynamical pathway consistent with these findings is dissociation of a binary asteroid during a close encounter with a planet and we confirm its plausibility using $N$-body simulations. We thus conclude that both the dynamical and spectroscopic properties of 474640-2013 $\mathrm{RF}_{98}$ favour a genetic link and their current orbits suggest that the pair was kicked by a perturber near aphelion.


Key words: techniques: photometric-techniques: spectroscopic-astrometry-celestial mechanics - minor planets, asteroids: individual: (474640) $2004 \mathrm{VN}_{112}$ - minor planets, asteroids: individual: $2013 \mathrm{RF}_{98}$.


Figure 2. Final visible spectra of the pair of ETNOs (see the text for details).


Figure 3. Comparison between the spectra of (474640) $2004 \mathrm{VN}_{112}$ and 2013 RF $_{98}$ smoothed by a Savitzky-Golay filter (see the text) and scaled to match at $0.60 \mu \mathrm{~m}$. The most prominent absorption band of pure methane ice at $0.73 \mu \mathrm{~m}$ is not seen on either spectra.


Figure 4. Evolution of the angular separation between the orbital poles of the pair (474640) $2004 \mathrm{VN}_{112}-2013 \mathrm{RF}_{98}$ for three representative test calculations with different perturbers. Red: $a=549 \mathrm{au}, e=0.21, i=47^{\circ}$ and $m$ $=16 M_{\oplus}$. Blue: $a=448 \mathrm{au}, e=0.16, i=33^{\circ}$ and $m=12 M_{\oplus}$. Green: $a=$ $421 \mathrm{au}, e=0.10, i=33^{\circ}$ and $m=12 M_{\oplus}$.
iment). Our preliminary results indicate that a planet with mass, $m$, in the range $10-20 M_{\oplus}$ moving in an eccentric (0.1-0.4) and inclined $\left(20-50^{\circ}\right)$ orbit with semimajor axis of $300-600$ au, may be able to induce the observed tilt on a time-scale of 5-10 Myr. Per-

## Consistent with the Planet Nine hypothesis?

Assuming a mass, $m$, in terms of the mass of the Earth:
if $m$ is in the range 10 to 20 Earth masses

- Semi-major axis (200 AU + $30 \mathrm{~m}, 600 \mathrm{AU}+20 \mathrm{~m}$ ) (300 AU, 600 AU )
- Eccentricity $=0.75-((250 \mathrm{AU}+20 \mathrm{~m}) / \mathrm{a})^{8}$
(0.1, 0.4)
- Inclination ( $22^{\circ}, 40^{\circ}$ ) ( $20^{\circ}, 50^{\circ}$ )
- Longitude of the ascending node $\left(72^{\circ}, 121^{\circ}\right)$
- Argument of perihelion $\left(120^{\circ}, 160^{\circ}\right)$


## Kreutz Sungrazers: The ultimate case of cometary fragmentation and disintegration?

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Table 6
Overview of Perturbations of Orbital Elements of Fragments Due to Separation Velocity of $\sim 5 \mathrm{~m} / \mathrm{s}$

| Fragments that are products of a breakup... | ....Reach next perihelion ... | ... In orbits that are ... |
| :---: | :---: | :---: |
| at or shortly after perihelion | at vastly different times (up to 2 millennia apart) | identical in $\omega, \Omega, i$, and $q$, but very different in $P$ |
| near 1 AU after perihelion | less than 1 century apart | slightly different in $\omega, \Omega, i\left(\$ 1^{d}\right)$, and $q\left(<0.01 R_{\odot}\right)$, but moderately different in $P$ |
| at a heliocentric distance of tens of AU after perihelion | tens of years apart | somewhat different in $\omega$, $\Omega$ (both up to a few deg), $i$ (up to $\sim 1^{\circ}$ ), $q$ (up to $\sim 0.1 R_{\odot}$ ), but fairly similar in $P$ |
| at a very large heliocentric distance preaphelion | several years apart | significantly different in $\omega, \Omega$ (both $\sim 10^{\circ}$ ), $i$ (a few deg), and $q$ (up to $\sim 0.5 R_{\odot}$ ), but only slightly different in $P$ |
| in the general proximity of aphelion | 1 year or less apart | very different in $\omega, \Omega, i$, and $q$, but nearly identical in $P$ |
| after aphelion | nearly simultaneously, not more than some weeks apart | determined by approximate symmetry of perturbations relative to aphelion, except for those in perihelion time |



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Figure 3: Differences between the values of the heliocentric orbital elements of the members of the initially bound binary at the end of the simulation. Bound pairs are plotted in green, unbound couples in red; the blue points show the actual values for the pairs of ETNOs (474640) $2004 \mathrm{VN}_{112}-2013 \mathrm{RF}_{98}(\Delta a=32.6 \mathrm{AU}), 2002 \mathrm{~GB}_{32}-2003 \mathrm{HB}_{57}(\Delta a=51.9 \mathrm{AU})$, (82158) $2001 \mathrm{FP}_{185}-2013 \mathrm{UH}_{15}(\Delta a=54.8 \mathrm{AU})$, and (148209) $2000 \mathrm{CR}_{105}-2010 \mathrm{~GB}_{174}$ $(\Delta a=143.1 \mathrm{AU})$. The results of 200000 experiments are plotted.

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# PAIRS AND GROUPS OF GENETICALLY RELATED LONG-PERIOD COMETS AND PROPOSED IDENTITY OF THE MYSTERIOUS LICK OBJECT OF 1921 

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#### Abstract

We present the history of investigation of the dynamical properties of pairs and groups of genetically related longperiod comets (other than the Kreutz sungrazing system). Members of a comet pair or group move in nearly identical orbits, and their origin as fragments of a common parent comet is unquestionable. The only variable is the time of perihelion passage, which differs considerably from member to member owing primarily to an orbitalmomentum increment acquired during breakup. Meter-per-second separation velocities account for gaps of years or tens of years, thanks to the orbital periods of many millennia. The physical properties of individual members may not at all be alike, as illustrated by the trio of C/1988 A1, C/1996 Q1, and C/2015 F3. We exploit orbital similarity to examine whether the enigmatic and as-yet-unidentified object discovered from the Lick Observatory near the Sun at sunset on 1921 August 7 happened to be a member of such a pair and to track down the longperiod comet to which it might be genetically related. Our search shows that the Lick object, which could not be a Kreutz sungrazer, was likely a companion to comet $\mathrm{C} / 1847 \mathrm{C} 1$ (Hind), whose perihelion distance was $\sim 9 R_{\odot}$ and true orbital period was approximately 8300 yr . The gap of 74.4 yr between their perihelion times is consistent with a separation velocity of $\sim 1 \mathrm{~ms}^{-1}$ which sets the fragments apart following the parent's breakup in a general proximity of perihelion during the previous return to the Sun in the seventh millennium BCE.


Key words: comets: general - methods: data analysis

Table 1
Orbital Elements of Comets C/1988 F1 (Levy) and C/1988 J1 (Shoemaker-Holt) (Equinox J2000.0)

| Orbital Element/Quantity | Comet C/1988 F1 | Comet C/1988 J1 |
| :---: | :---: | :---: |
| Osculation epoch (TT) | 1987 Nov 21.0 | 1988 Feb 9.0 |
| Time of perihelion passage $t_{\pi}$ (TT) | 1987 Nov 29.94718 | 1988 Feb 14.22162 |
| Argument of perihelion $\omega$ (deg) | 326.51491 | 326.51498 |
| Longitude of ascending node $\Omega$ (deg) | 288.76505 | 288.76487 |
| Orbit inclination $i$ (deg) | 62.80744 | 62.80658 |
| Perihelion distance $q$ (au) | 1.1741762 | 1.1744657 |
| Orbital eccentricity $e$ | 0.9978157 | 0.9978301 |
| Orbital period $P(\mathrm{yr})\left\{\begin{array}{l}\text { osculation } \\ \text { original }^{\text {a }}\end{array}\right.$ | $\begin{gathered} 12,460 \pm 460 \\ 13,960 \end{gathered}$ | $\begin{gathered} 12,590 \pm 230 \\ 13,840 \end{gathered}$ |
| Orbital arc covered by observations | 1988 Mar 22-1988 Jul 18 | 1988 May 13-1988 Oct 20 |
| Number of observations employed | 30 | 60 |
| rms residual (arcsec) | $\pm 0.7$ | $\pm 0.9$ |
| Orbit-quality code ${ }^{\text {b }}$ | 2A | 2A |
| Reference | Marsden (1989b) | Marsden (1989b) |

Notes.
${ }^{\text {a }}$ Referring to the barycenter of the solar system.
${ }^{\mathrm{b}}$ Following the classification system introduced by Marsden et al. (1978); the errors of the elements other than the orbital period are unavailable.

## Planets beyond Pluto?

In brief, the existence of significant anisotropies in the distributions of the directions of perihelia and poles of the ETNOs is the main observational fact used to argue in favour of the presence of trans-Plutonian planets. The very same argument, but making use of comet data, has been proposed multiple times during the last ten decades or so to claim new planetary discoveries. Each and every one of these propositions was eventually dismissed as induced by strong observational bias. These historical precedents may lead us to ask, why is this time going to be any different? The answer is in the data.

## Planets beyond Pluto?

## RND THE DRTP

 5月Y, YES!
## Planets beyond Pluto?

Neptune was predicted using pen and paper; computers are leading the way to the trans-Plutonian Planets.

## Updates

https://www.researchgate.net/ project/Trans-PlutonianPlanets

